### THE NATURE OF TIME

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**Abstract.** A review of some basic facts of classical dynamics shows that time, or precisely duration, is redundant as a fundamental concept. Duration and the behaviour of clocks emerge from a timeless law that governs change.

#### 1 Introduction

My library contains four books on mechanics, the science of change in time. Three of them – all modern classics – fail to define either time or clocks! Relativity textbooks do discuss time and clocks but concentrate on only one of the two fundamental problems of time that Poincaré identified in 1898 [1]: the definitions of duration and of simultaneity at spatially separated points. Since then the first problem has been remarkably neglected, probably because Einstein's solution of the second in 1905 created such excitement.

The failure to discuss duration at a foundational level largely explains the unease many feel when confronted with the idea that the quantum universe is static. This suggestion emerged in 1967 from a rather high-level attempt by Bryce DeWitt [2] to meld Einstein's classical general theory of relativity with quantum theory and has given rise to decades of agonizing over 'the problem of time'. In my view, had duration been properly studied in classical physics, its disappearance in the conjectured quantum universe would have appeared natural. In this essay I will not discuss quantum theory but instead question the standard assumptions made about duration in classical physics.

I shall develop from scratch a theory of time and clocks, linking it to work that astronomers began in antiquity. The best guide to the nature of time is the practice of astronomers. They cannot afford mistakes; a missed eclipse is all too obvious. Moreover, they work directly with concrete observations, not obscure metaphysical notions of time.

My discussion begins with Newton's comments on astronomical practice in his great Mathematical Principles of Natural Philosophy (1687), my only book on mechanics that does discuss duration. Newton's discussion leads directly to two key intimately related questions: How can we say that a second today is the same as a second yesterday? What is a clock? The answers to these questions, which are seldom addressed at a sufficiently foundational level, will tell us much about time and the way the physical world works. We shall find answers to them by examining successive important discoveries made over two millennia.

I hope the answers to the two questions will persuade you that time as an independent concept has no place in the foundations of physics. It arises from something concrete but deeper. As Ernst Mach said (1883) [3]:

It is utterly beyond our power to measure the changes of things by time ... time is an abstraction at which we arrive by means of the changes of things; made because we are not restricted to any one definite measure, all being interconnected.

Einstein, an admirer, quoted this passage in his obituary of Mach, calling it a gem. Oddly, Einstein never directly attempted a Machian theory of time, but in fact such a theory of 'time without time' sits hidden within the mathematics of his general theory of relativity [4], the foundation of modern classical physics.

The time-without-time foundation of classical physics entails a relatively small adjustment to our conceptions, but is likely to have a profound effect in a quantum theory of the universe. This is because significant parts of classical physics, above all time, are carried over unchanged into quantum theory. If our ideas about time in classical physics are wrong, surprises can be expected in a quantum theory of the universe. As of now, little can be said about this with certainty because no such theory yet exists. The very idea could even be wrong. Nevertheless, tentative theories have been proposed. The one I favour seems initially impossible: the quantum universe is *static*. Nothing happens; there is being but no becoming. The flow of time and motion are illusions.

As I have said, I find this natural, but I shall not here describe my vision of a timeless quantum universe presented in *The End of Time* [5]. Instead, using a few elementary equations and some new arguments, I wish to strengthen the case for eliminating time as a fundamental concept in classical physics. The arguments are simple. They strongly suggest that time should be banished. Writing about the nature of time is a hard task. Unlike the Emperor dressed in nothing, time is nothing dressed in clothes. I can only describe the clothes.

## 2 The Theory of Duration

## 2.1 Newton and the Equation of Time

No essay on time can omit Newton's magisterial words:

Absolute, true, and mathematical time, of itself, and from its own nature, flows equably without relation to anything external, and by another name is called duration: relative, apparent, and common time, is some sensible and external measure of duration by the means of motion, which is commonly used instead of true time; such as an hour, a day, a month, a year.<sup>1</sup>

Newton here implies that in some given interval of true time the universe could do infinitely many different things without in any way changing that interval of time. This view still sits deep in the psyche of theoretical physicists and is only partly exorcized from general relativity. I shall show that intervals of time do not pre-exist but are *created by what the universe does*. Indeed, Newton can be hoist with his own petard if we see what his marvelous laws actually tell us.

Let us start with his concession to practicality: the relative time, which we are forced to use, is found "by the means of motion". Moreover, the measures are concrete: shadows mark the hours on a sundial; the moon waxes and wanes; the seasons pass. They are almost as tangible as Shakespeare's "daisies pied and violets blue" that come with the cuckoo. They are all clothes of time.

But what does Newton tell us about time itself, his ultimate absolute along with space? Can you get your hands on time? He is more aware of the question and a potential answer than many modern authors:

Absolute time, in astronomy, is distinguished from relative, by the ... astronomical equation. The necessity of this equation, for determining the times of a phenomenon, is evinced as well from the experiments of the pendulum clock, as by eclipses of the satellites of Jupiter.

The 'astronomical equation' is today called the *equation of time* and is the correction that equalizes – hence 'equation' – the times measured by the sun or the stars. It is important for my argument and so needs to be explained. The successive returns of the sun and a given star to due

<sup>&</sup>lt;sup>1</sup>For readers finding difficulty with Motte's 1729 translation of Newton's Latin, equably means uniformly and sensible means observable (through the senses).

south at the Greenwich Observatory define the *solar* and *sidereal* days respectively. The first is on average four minutes longer than the second because the sun moves eastward relative to the stars along the great circle on the sky called the *ecliptic* (eclipses can only occur when the moon too is on the ecliptic). Superimposed on the average sidereal—solar difference are two effects. The sun's speed along the ecliptic (measured by either day) is not exactly constant. This reflects the earth's variable speed in its orbit around the sun. Second, when the sun is high in the sky in the summer and low in the winter, its motion along the ecliptic is purely eastward relative to terrestrial south, and the sidereal—solar difference is enhanced compared with the spring and fall, when this is not the case. The two effects, well known in antiquity, cause solar time to be sometimes ahead and sometimes behind sidereal time by about 15 minutes. Is there some reason to choose one of these times in preference to the other?

When Ptolemy wrote the *Almagest*, the compendium of ancient astronomy, around 150 CE, he knew no modern laws of motion. In his rudimentary astronomy the sun, moon, planets, and stars were all carried around the earth in curiously different ways. Since the sun outshone everything in the heavens, dominated life, and governed civil order, he could have taken it to measure time. In fact, he chose the stars; his reason is instructive and marks the first step to a theory of duration.

He and his great predecessor Hipparchos (who flourished around 150 BCE) had developed a theory of the motion of the sun and the moon around the earth. Its key element was uniform motion of both the sun and moon around certain circles. It predicted eclipses of the moon with reasonable accuracy provided the motion in the circles was taken to be uniform relative to sidereal time. Because 15 minutes are significant in eclipse prediction, the sidereal—solar fluctuations ruled out the sun as the hand of time. What can we learn from this? In his mind's eye, Ptolemy could 'see' the stars, sun, and moon moving in their circles. It is the way they move, specifically the correlations between their motions, that warrants the introduction of a distinguished measure of time. Ptolemy's choice of sidereal time to measure duration remained unchallenged for close on two millennia.

This is the justification of Newton's comments about the astronomical equation. The earth's rotation was still by far the best measure of time in his day, but astronomical knowledge had been greatly extended, above all by Kepler's laws. The pendulum clock had also been invented, and experiments confirmed that it – and the satellites of Jupiter – marched better in step with sidereal than solar time. In fact, Newton actually says that [absolute] duration is to be distinguished "from what are only sensible measures thereof ... by means of the astronomical equation". This statement is both important and ironic; important in confirming that the measure of time is not chosen before but after the discovery of specially correlated motions, ironic because the motion of the stars is just as 'sensible a measure' as any other. As Newton himself defines it, absolute time is by no means independent of the world; it is a specific motion, the rotation of the earth.

#### 2.2 The Changes of Things, All Interconnected

Two comments before we proceed. Since time must be deduced from change of position (motion), I shall here take position and differences of position as given, though great issues do lurk behind these apparently simple notions [6]. Second, clocks are of two kinds: natural like the earth's rotation and man made. Because man-made clocks are complex and rely on special devices, they do not reveal the nature of time and the basis of time keeping as well as natural clocks. For example, we shall see that the often made statement that a periodic process is the basis of a clock is misleading.

The development of astronomy in the period from Newton to the end of the 19th century nicely illustrates Mach's words recalled above. For the sake of a telling image, let us 'simplify' the solar

system and suppose all the planets revolve around the sun in one plane; that the earth's rotation axis is perpendicular to that plane; and that astronomers observe them against the background of the stars from a 'crow's nest' very far 'above' the sun. From it they can observe directly: the distances  $r_i$  of each planet i from the sun; the angle  $\phi$  through which the rotating earth turns relative to a fixed star ( $\phi$  measures terrestrial sidereal time); the angles  $\alpha_i$ , i = 1, 2, ..., between the lines from the sun to each planet i and a fixed star. Modern textbooks, leaving us to fathom the meaning of t, say that all these quantities are functions of the time:  $\phi(t)$ ,  $\alpha_i(t)$ ,  $r_i(t)$ . But Newton effectively identified time with sidereal time, i.e., the angle  $\phi$ . In reality the Newtonian specification of each observed configuration of the solar system is  $\alpha_i(\phi)$ ,  $r_i(\phi)$ , i.e., certain values of  $\alpha_i$  and  $r_i$  for each value of  $\phi$ . The undefined t plays no role.

Now we have to ask why the earth's rotation angle plays such a distinguished role. The earth can hardly be the lord of the planets' dance. Why not some other motion? Two great discoveries cast light on this question and did for a while bring in other special motions as candidates for the measure of time.

On Easter Sunday 1604 Kepler's immense labour finally crystallized in his first two laws of planetary motion: the planets move in ellipses with the sun at one focus; the line from the sun to each planet sweeps out equal areas in equal times as measured by  $\phi$ . We now have something special. The motions of the planets could have been arbitrary, but no: they exhibit remarkable correlations. The areas swept out by the planets and the earth's rotation all march in step. They 'keep the same time'. Moreover, the correlations are only found between certain motions; there are no clean correlations between the varying planet—sun distances  $r_i$ .

The second discovery, unthinkable without Kepler, was Newton's laws of motion and universal gravitation. His first theorem in the *Principles* uses Kepler's area law to prove that all the planets are deflected from their natural inertial motion by a force that tugs them toward the sun. And what measure now does Newton take as time to find the acceleration, the second time derivative, generated by this centripetal force? In one truly beautiful geometrical proof, he takes advantage of the further specially correlated motions found by Kepler and uses, not the earth's  $\phi$ , but the area swept out by the very planet whose acceleration he is determining. Newton had discovered dynamics. Wonderfully simple laws governed all motions in the heavens and on the earth.

But had he caught time? Clearly no, but still a great catch: diverse and special precisely correlated motions and a law of gravitation that gave the observed accelerations relative to these motions. Newton was wrong to go beyond this fact, tempting though it was to 'see' the invisible structure of time behind its clothes.

Mach in contrast was right: we do abstract time from motion. It only seems to be a universal absolute "because we are not restricted to any one definite measure, all being interconnected". For Newton's purposes, the area swept out by a planet was as good as  $\phi$ . But then it turned out that this is not strictly true. In accordance with Newton's laws and as confirmed observationally in the 18th and 19th centuries, the planets perturb each other's motions. Their orbital areas do not march *perfectly* in step with  $\phi$  or with each other. Remarkably, using  $\phi$ , the 'sensible' hand that Newton had ironically identified as absolute time, the calculated perturbations matched the observations perfectly. The astronomers were lucky; no man-made clock could remotely rival the earth's rotation at that time.

This happy situation persisted until the 1890s, when a crisis developed whose resolution takes us deeper into the nature of time.

### 2.3 The Acceleration of the Moon and Ephemeris Time

The moon moves across the stellar sky faster than the other celestial bodies and is much easier to observe and use to test Newton's laws. In the 1890s, astronomers came to the uncomfortable conclusion that the moon exhibited a small but undeniable non-Newtonian acceleration. What could be the cause? They wondered whether the earth might absorb the sun's gravity during eclipses of the moon and allow the anomalous acceleration, or whether the moon's tidal effects could be slowing the earth's rotation.

Most astronomers correctly guessed the latter but then had to seek a better and more fundamental measure of time. I shall argue that, perhaps without realizing it, they implicitly asked the ultimate question: what is time? As Poincaré described it in his important paper [1], they proceeded as follows. Suppose Newton's laws are correct and the solar system is a closed dynamical system, i.e., no external objects exert significant disturbing forces on it. Then it must be possible to define a time variable such that Newton's laws do hold for the solar system when it is used. The astronomers defined time so as to ensure that the laws hold [7].

There is a short cut that enables us to 'see' this time. It exploits a fundamental concept: the energy of a system. Here we need the equations. Mutually gravitating bodies have potential energy

$$V = -G\sum_{i < j} \frac{m_i m_j}{r_{ij}},\tag{1}$$

where G is Newton's gravitational constant,  $m_i$  is the mass of body i in the system, and  $r_{ij}$  is the distance between bodies i and j. The summation symbol  $\sum$  with i < j under it means take all pairs ij once, calculate  $m_i m_j / r_{ij}$  for each, and add them all together.

The bodies also have kinetic energy T, which is simply the sum of the kinetic energies of each body (half its mass  $m_i$  times the square of its speed  $v_i$ ). I want to write this in the most revealing way. The Greek letter  $\delta$  before some symbol, say d for distance, means  $\delta d$  is very small. Now suppose that, in the small time  $\delta t$  to be defined, body i moves the distance  $\delta d_i$ . Then to a good approximation its speed is

 $v_i = \frac{\delta d_i}{\delta t},$ 

and

$$T = \sum_{i} \frac{m_i}{2} \left( \frac{\delta d_i}{\delta t} \right)^2,$$

where now the contributions of each particle are added.

Perhaps the most fundamental result in dynamics is that the energy T + V of an isolated system remains exactly equal to a constant E in time. One says that the energy is conserved. This is normally expressed by the equation

$$\sum_{i} \frac{m_i}{2} \left(\frac{\delta d_i}{\delta t}\right)^2 + V = E,\tag{2}$$

where V is given by (1).

Suppose the astronomers in the crow's nest take 'snapshots' of the solar system in successive configurations. Each gives directly the separations  $r_{ij}$ , and from two taken in quick succession the  $\delta d_i$  can be found. If the astronomers had a clock with them, they could test the law (2). But in the 1890s they had no adequate clock. What they effectively did was rearrange (2) and use it to

define the increment  $\delta t$  of time between successive configurations:

$$\delta t = \sqrt{\frac{\sum_{i} m_{i} (\delta d_{i})^{2}}{2(E - V)}}.$$
(3)

The time derived from (3) is called *ephemeris time* [7]; an ephemeris gives the positions of celestial bodies, and  $\delta t$  is deduced from such positions. We are now in a position to define a manmade clock, a *chronometer*: "it is a mechanism for measuring time that is continually synchronized as nearly as may be with ephemeris time" [7]. The astronomer Clemence was led to propose this definition in 1957 because he found that many authors writing about relativity have "no clear idea of what a clock is."

Apart from the constants G and E and  $m_i$ , which I shall discuss shortly, (3) contains only displacements and distances. According to it, the instantaneous speed of particle i is

$$v_i = \frac{\delta d_i}{\delta t} = \sqrt{\frac{2(E - V)}{\sum_i m_i (\delta d_i)^2}} \, \delta d_i.$$
 (4)

The  $\delta t$  appearing here in  $\delta d_i/\delta t$  is merely shorthand for (3), and the expression on the right is the one that counts. The elusive t has been eliminated. Science should deal with observable things, so this is a step forward. Equation (4) expresses the truth that only relative quantities have objective meaning. Speed of body i is not the ratio of its displacement to an abstract time increment but to (3), which involves the displacements of all the bodies in the system.

I regard the definition of duration by (3) as exceptionally important for two reasons: it is made possible solely because the bodies in the system move in a very special way (duration does not 'pre-exist' that fact as Newton asserted); time is no longer measured by particular individual motions but by the sum of all motions.

There is however still some work to do to get that time concretely. If the astronomers know the values of G, E, and  $m_i$  in advance, two 'snapshots' taken of the solar system in quick succession will suffice to determine the  $\delta t$  between them. If they do not, a sufficient number must be taken to provide enough data for their determination. The 'time' (3) will then truly emerge from observed positions of objects. Time can be read off the heavens.

Valuable as is the astronomers' notion of ephemeris time, the principles behind it are still somewhat vague. The astronomers start with a theory formulated in terms of an undefined time and then use observations to define it. I want to show in the remainder of the paper that this obscures the truth. It is evident from what I have so far presented that one could never speak about a time worthy of the name were it not for the wonderfully correlated motions that nature exhibits. What we really need is a *timeless* theory of the correlations. Before providing that I want to make clear just how remarkable the correlations are. This will have the advantage of highlighting the difference between Einstein's definition of a clock and Clemence's [7].

#### 3 Contrasted Definitions of Clocks

An important question that we have not yet considered is how *natural* clocks can march in step. By Clemence's definition, man-made chronometers will do that through human artifice since they must all be synchronized to the solar-system ephemeris time.<sup>2</sup> A point that I want to make now is

<sup>&</sup>lt;sup>2</sup>In fact, it is now atomic time. Astronomers replaced sidereal time by ephemeris time only in 1952 and then introduced atomic time in 1979.

that, from the fundamental perspective, it is a mistake to concentrate on the definition of a single clock. Clocks are useless if they do not march in step for otherwise we cannot keep appointments. Therefore it is not a clock that we must define but clocks and the correlations between them as expressed in the marching-in-step criterion. We shall see that this leads to a very different definition of clocks – and understanding of time – to that of Einstein, given below.

A crucial role in the definition of natural clocks is played by the term E - V in (3). To my knowledge, its significance, though rather obvious, has not hitherto been noted. We imagined our astronomers 'looking down' on the solar system. Suppose that far 'above them' is another system, similar but not identical. Its energy E and the masses of its bodies will be different. Suppose the astronomers take simultaneous snapshots of the two systems at successive instants and want to determine the time interval between the instants from the snapshots. Now in general the value they obtain of  $\delta t_2$  will not be equal to  $\delta t_1$  because the quantities that go into (3) for the two systems can be very different. However, the two systems will be good clocks if in any interval the ratio  $\delta t_2/\delta t_1$  is always the same. For then they march in step but merely take larger steps like the tips of ticking second hands of unequal lengths.

It is here that E-V comes into play. In isolated dynamical systems, including the gravitational ones we are considering, the kinetic energy T and potential energy V are constantly changing, but their sum E=T+V remains constant – the total energy is conserved. As a result, if T gets larger, so does E-V. This is now crucial for the way our two 'clocks' behave. If T for system 1 becomes relatively larger than T for system 2, the numerator in (3) of system 1 will be boosted compared with system 2 but the denominators will counteract the effect; the ratio  $\delta t_2/\delta t_1$  will always be same, and the two 'clocks' will keep step. This will be true for any number of systems.

Thus, natural clocks are isolated dynamical systems with hands that are advanced in accordance with (3); the law that governs their behaviour – which I have still to spell out in timeless form – ensures the marching-in-step condition.

Finally, in reality there is no *perfectly* isolated system except the entire universe. In a Newtonian picture, it could be the multitudinous stars of our Galaxy in otherwise infinite space. Of course, in such a universe there can be innumerable effectively isolated systems and as many synchronous ephemeris times.

We see from this that time has no role to play as an independent element of reality. It can be abstracted from change. However, Mach could have been more specific – the definition of time must be based on an accurate description of the way naturally occurring motions are correlated. Ptolemy's successful epicycle theory selected sidereal time in preference to solar time; equally Newton's success with his dynamical laws justified his claim that 'absolute time' could be deduced from the astronomical equation. When we push our understanding to the limit, we arrive at the ephemeris time (3) with its reduction of time to masses, displacements, separations, and the constants E and G. Even in Einstein's much more sophisticated general relativity time emerges in much the same way [4].

The theory of duration and clocks that emerges from observable differences as made explicit in (3) is very different from the view that prevailed among the great relativists in the early 20th century. It will suffice to consider Einstein's definition of clock in 1910 [8]:

By a clock we understand anything characterized by a phenomenon passing periodically through identical phases so that we must assume, by the principle of sufficient reason, that all that happens in a given period is identical with all that happens in an arbitrary period.

I see several problems with this definition. First no system ever runs through truly identical phases, so this is an idealization that hides the true nature of time; it lacks Poincaré's insistence

[1], which I have repeated, that only the universe and all that happens in it can tell perfect time. Second, Einstein's clock cannot measure time continuously. It can only indicate that a given interval has elapsed when identical phases recur. It can say nothing about the passage of time in intervals within phases. Since the universe is the only perfect clock, it seems nothing at all can be said about the passage of time unless there is recurrence of eons under identical conditions. Even then one can only say that the eons are equally long. In contrast, the ephemeris time defined by (3) runs continuously and in no way relies on recurrence of identical phases. Finally, by relying on periodicity, Einstein's definition fails to identify the true dynamical basis of time keeping and the importance of understanding why clocks can march in step.

Now to the timeless law that explains how billions upon billions of natural clocks scattered through the vast reaches of space can all tick in step.

# 4 The Timeless Principle of Least Action

The configuration space of the universe is the key concept. In a universe of N particles, each particle position has 3 coordinates; 3N define a complete configuration, which corresponds to a unique representative point p in an abstract 3N-dimensional space  $\mathcal{U}$ . As the universe's configuration changes, p traces a curve in  $\mathcal{U}$ . If the universe were to follow some arbitrary curve, no law would hold. The remarkably simple and beautiful principle of least action singles out the special curves in  $\mathcal{U}$  for which Newton's laws hold. I shall present it in a little-known timeless form: Jacobi's principle.

You choose in  $\mathcal{U}$  two points – two configurations of the universe. These are to remain fixed. You consider all possible *trial curves* that join them continuously in  $\mathcal{U}$ . In the usual formulation, all trial curves are assumed to be traversed in a fixed pre-existing time interval. No such assumption is made here; it is unnecessary. All you need to do is divide each trial curve into very short segments. For each segment, you calculate its *action* 

$$\delta A = \sqrt{2} \sqrt{\left(E - \sum_{i < j} \frac{m_i m_j}{r_{ij}}\right) \sum_i m_i (\delta d_i)^2},$$
(5)

where  $\delta d_i$  is the distance particle *i* has moved. Here *E* is not regarded as an energy but as a fundamental constant (like the cosmological constant  $\Lambda$  [4]). The action *A* for the complete trial curve is the sum of the actions  $\delta A$  for each segment; in the limit in which the segments are made shorter and shorter, *A* tends to a finite limit.

Now comes the wonderful thing. For one of the trial curves, the action will be smaller than for any other. For this extremal curve, and in general for no other joining the fixed end points, the particles obey Newton's laws with the emergent time defined by (3). This is a timeless law; it determines a path, or history, in  $\mathcal{U}$ . The key thing is that no time is assumed in advance. A time worthy of the name does not exist on any of the non-extremal curves. Time emerges only on the extremal curves.

It is not only Newton's laws that can be obtained in this timeless way. There is an interpretation of Einstein's general relativity in which it and time arise in much the same way [4]. I will not claim that time can definitely be banished from physics; the universe may be infinite, and black holes present some problems for the timeless picture. Nevertheless, I think it is entirely possible – indeed likely – that time as such plays no role in the universe.

Occam's razor tells us to avoid redundant elements. All we need are differences. Indeed, the passage of time is always marked by difference, often seen as cruel:

When forty winters shall besiege thy brow, And dig deep trenches in thy beauty's field, Thy youth's proud livery, so gazed on now, Will be a tattered weed of small worth held.

Unlike Newton, Shakespeare did not attempt to describe time itself, only the differences associated with it. Look again at the 'expression for time':

$$\delta t = \sqrt{\frac{\sum_{i} m_{i}(\delta d_{i})^{2}}{2(E - V)}}.$$

Some of those  $\delta d_i$ s are the trenches dug in youth's brow.

## References

- [1] Poincaré H "La mesure du temps," Rev. Métaphys. Morale 6 1 (1898); English translation: "The measure of time," in: Poincaré H The Value of Science
- [2] DeWitt B S "Quantum theory of gravity. I. The canonical theory," Physical Review 160 1113 (1967).
- [3] Mach E The Science of Mechanics, Open Court (1960) (translated from the German)
- [4] Barbour J, Foster B, and Ó Murchadha N "Relativity without relativity," Class. Quantum Grav. 19, 1571 (2002) (gr-qc/0012089).
- [5] Julian Barbour, The End of Time, Oxford University Press, New York (2000).
- [6] Julian B Barbour, The Discovery of Dynamics, Oxford University Press, New York (2001).
- [7] Clemence G M "Astronomical time"  $Rev.\ Mod.\ Phys.\ \mathbf{29}$  2 (1957).
- [8] Einstein A, "Principe de relativité" Arch. Sci. Phys. Natur., ser. 4. 29 5 (1910).